ABSTRACT: The Optimization of various aero engine components has a very big role in effective development of modern aircrafts. In the current project, the rotating compressor disk is the component chosen for shape optimization. The problem of this study is that consideration of aero engine disc that works with a high rotational velocity at elevated temperatures. The compressor disk is analyzed in ANSYS APDL tool to get stress outputs and the results are calculated analytically. The FEA model of the disc is modeled in an analysis tool ANSYS and analysis is carried out to get stress output. Calculating the burst margin for every result output. Selecting the best optimum result by consideration of minimum disk mass and burst margin increment obtained during the analysis.

KEYWORDS: Aircraft Engine, Shape Optimization, ANSYS APDL, Compressor Disc.

I. INTRODUCTION

A compressor disc is a very important component in an aircraft engine. The work of the compressor is to convert the kinetic energy of the fluid or air passing through it to potential energy, this process is done by compressing the fluid passing through it. After compression the fluid is made to pass to the combustion chamber where the fuel is burnt in the engine and the hot gases flows through turbine blades to rotate it. In the operation the aero engine must sustain a huge load. Due to a very high rotary speed and high temperatures of about 300°- 500° Celsius. These various loads imposes huge amount of stresses in the engine parts and also the compressor disc. At first the initiation of static cracks takes place in the disc and then the cracks grow vigorously resulting in failure the of compressor disc. The bursting of the compressor disc may lead to failure of the aircraft engine creating dangerous circumstances in an air craft.

Burst speed is the rotational speed of the compressor disc at which the disc starts to yield. The burst margin is the range of rotational speed at which the compressor disc can operate safely without yielding. The discs in the aero engine constitutes of about 25-30 % of mass in the overall engine’s weight. Reducing the weight of the compressor disc is very important to improve the efficiency and performance of the aero engines. In the current project work, the shape optimization of the compressor disc is done. The optimization of disc can reduce the mass of the disc with more strength. This increases the weight to thrust ratio of the engine, and also plays a major role on the weight deciding factor for other components like shafts and blades. The compressor disc is designed and simulated with the help of analysis software “ANSYS MAPDL V15”. A typical compressor disc is designed with appropriate dimensional tolerances. In modern days the computational FEA method became handy and alternative method in product development process of various components and products in various industries typically in the aircraft industries. The more expensive it becomes for the experimental setups compared to the numerical and analytical methods like FEA.

The problem of the project work is to optimize the compressor disc by getting a safe design of the disc. Since in a rotating object, the major force acting is the centrifugal force along with thermal stresses. Because of that the engine disc bears a vast mechanical load. The speed of the engine should be increased more than the maximum one hundred percentages in several occasions during the flight, because to this reason the engine disc also should sustain the extra load imposed on it during flight without undergoing failure. Burst margin is the range of rotational speed that a compressor disc works without undergoing yielding. The burst margin is the range of rotational speed at which the compressor disc can operate safely without yielding. The minimum disc mass an optimized burst margin is considered as the criteria for the current project. The bore radius, bore width, bore angle and diaphragm width is the variable parameters which are varied during the shape optimization of compressor disc. With a FEA model of the disc, the
optimization for burst margin and weight reduction for a compressor disc is carried out in this project. The results are matched with analytical calculations.

II. METHODOLOGY

(a) Material description

In the project work, the material used has material properties of young’s modulus about 110 GPa at 420° Celsius, the poison’s ratio is 0.3. The density of the material is 4.1 kg/m³. The ultimate tensile strength (UTS) is 725 MPa. The angular velocity of the rotating disc is 14005.5 RPM. The specifications and properties of the material are not disclosed by the organization. They provided the data which are required for the analysis. The material properties of the material used is provided in the table 1.

Material properties of the model

<table>
<thead>
<tr>
<th>Temperature</th>
<th>420° Celsius</th>
</tr>
</thead>
<tbody>
<tr>
<td>Young’s modulus (E)</td>
<td>110 GPa</td>
</tr>
<tr>
<td>Poison’s ratio (υ)</td>
<td>0.3</td>
</tr>
<tr>
<td>Material Density</td>
<td>4.1 g/m³</td>
</tr>
<tr>
<td>Ultimate Tensile Strength</td>
<td>725 MPa</td>
</tr>
</tbody>
</table>

Analysis of a general regular shaped hollow rotating disc

Hollow disc which has regular normal cylindrical dimensions is considered to do analysis for validation process. In this sector the analysis is done out for hoop stresses and radial stress for a hollow disc which is a regular geometry. Here for the hollow disc stress analysis, the relevant mathematical expressions are available for manual calculations. The material properties given during the analysis in the tool are

| Young’s modulus (E) | 110 GPa |
| Poison’s ratio (υ) | 0.3 |
| Material Density | 4.1 kg/m³ |
| Ultimate Tensile Strength | 725 MPa |

The Area weighted mean hoop stress (AWMHS) calculation of for a disc is not possible without the help of an analysis tool. To calculate the AWMHS of the disc, every individual element with its average stress values are necessary. The hand calculation of hoop stresses for an irregular geometry is also very difficult, since the required mathematical expressions for an irregular geometry are not readily available. Hence, we are taking a normal regular geometry for validation. The actual project’s modeling is done in chapter 5, the actual dimensions of the compressor disc are considered for the design in the next chapter.

Dimensions of hallow disc

Case: The dimensions which are selected will suits the dimensions of the aero engine’s compressor disc which is selected for the shape optimization in the current project. A typical disc with regular geometry which resembles a cylinder is modeled in the ANSYS APDL tool and analyzed to get the stress values and hoop stress patterns.
Table 3: Dimensions of the hollow disc

<table>
<thead>
<tr>
<th>Disc dimensions</th>
<th>Dimensional range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bore inner radius (R₁)</td>
<td>130 mm</td>
</tr>
<tr>
<td>Bore width (h)</td>
<td>40 mm</td>
</tr>
<tr>
<td>Rim outer radius (R₂)</td>
<td>290 mm</td>
</tr>
</tbody>
</table>

Mass of the circular disc with hole

- Volume of the hollow disc
  \[ V = \pi \times h \times (R₁² - R₂²) \]
  \[ = \pi \times (40)\times(290² - 130²) \times 10^-6 = 8.14 \text{ mm}³ \]
- Mass of the hollow disc
  \[ M = V \times \rho \]
  \[ = 8.14 \times (4.1 \times 10⁻⁹) \times 10^⁹ = 34.60 \text{ KG} \]

(b) FEM analysis of the general hollow disc

The boundary conditions are given by constraining a node in the hollow in the ‘y’ direction. The inertial load of an angular velocity of 1466.66 radians/sec was given as the load in global ‘y’ direction. The disc is made to rotate perpendicular to the ‘y’ axis. The stress outputs and stress distribution patterns for hoop stress and radial stress values of the hollow cylinder is similar to the regular compressor disc. The following figures 1 and 2 represent the hoop stress patterns and the maximum hoop stress region of the hollow disc which approximately represents the actual compressor disc in the design.

![Fig 1: Maximum hoop stress and hoop stress distribution pattern of hollow disc](image1)

![Fig 2: Maximum radial stress and hoop stress distribution pattern of hollow disc](image2)
Therefore the results obtained from the solver during analysis are valid and matches the theoretical calculations. Since from the above analysis we have found that the magnitude of hoop stress generated in the disc is more than the radial stresses at the same speed, the further analysis will be carried out by considering the hoop stresses. If the design of the disc is safe for hoop stress, then the design will also be safe for the radial stress.

(c) Significant steps in simulation of compressor disc

The following flow chart shows the steps followed in the simulation of compressor disc for shape optimization to get optimum burst margin.
III. FINITE ELEMENT ANALYSIS OF THE MODEL

(a) Modeling of compressor disc

ANSYS 15 APDL tool is used for modeling and optimization is made by stress calculation. The following figure shows a typical 2d model of a compressor disc with labeling.

![Diagram of compressor disc](image)

**Fig 5: 2D model of the compressor disc**

In pre processing stage, the first step in 2d modeling of the compressor disc is to create the geometric entities like lines and areas in ANSYS 15 APDL tool. The lines and area are created by considering the minimum values of bore inner radius, bore width, bore angle and diaphragm width. Thus by creating lines of the desired geometry the area can be created further.

Dimensions of the disc

The table 4 gives the specifications of the dimensions of the disc and some of the selected dimensions will vary during the analysis for the optimization of the disc.

<table>
<thead>
<tr>
<th>Variable Dimensional parameter</th>
<th>Dimensional range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bore inner radius</td>
<td>135 mm – 145 mm (vary)</td>
</tr>
<tr>
<td>Rim Outer radius</td>
<td>300 mm</td>
</tr>
<tr>
<td>Bore width</td>
<td>30 mm – 40 mm (vary)</td>
</tr>
<tr>
<td>Bore angle</td>
<td>40° – 45° (vary)</td>
</tr>
<tr>
<td>Diaphragm width</td>
<td>7 mm – 9 mm (vary)</td>
</tr>
<tr>
<td>Bore Outer Radius</td>
<td>150 mm</td>
</tr>
<tr>
<td>Rim Width</td>
<td>20 mm</td>
</tr>
<tr>
<td>Rim Height</td>
<td>10 mm</td>
</tr>
<tr>
<td>Rim Angle</td>
<td>10°</td>
</tr>
</tbody>
</table>

(b) Creating lines with minimum dimensional values

Modeling of the compressor disc is done representing the lines in fig 6, the lines for a 2D model of the disc is drawn in ANSYS 15 APDL tool with appropriate dimensions.
The 2d model of the disc can be converted into a 3D model by axi-symmetric expansion of the compressor disc. The axi-symmetric expansion is done in the ANSYS 15 APDL tool, the optimization will be carried out with a 2d model of the disc. Since computer only understands the nodes and elements in an FEA tool the meshing is done for analysis. Meshing process in fem is the “conversion of geometric entities like lines, area, volumes into FE entities like nodes and elements”. In the current project meshing is also done in every case during the analysis. Because of the varying dimension of the model at each case, the meshing also must be done at each case. If the mesh density is very fine and size of the element is small, the computational time increases correspondingly. A fine mesh is necessary to get accurate results.

**PLANE182 Element**

PLANE182 element type in ANSYS is used for the 2-D modeling of solid structures. The element can be used as either a plane element or an Axi-symmetric element.
Mesh quality

<table>
<thead>
<tr>
<th>Element type</th>
<th>Quad node solid element</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of elements</td>
<td>3751</td>
</tr>
<tr>
<td>Average element area</td>
<td>4.365 mm²</td>
</tr>
<tr>
<td>Disc mass</td>
<td>10.6 KG</td>
</tr>
</tbody>
</table>

(c) Boundary conditions for the model
The boundary conditions to the model are given by fixing the disc in global ‘y’ direction. The disc is free to expand in other directions. One of the nodes in the disc is being fixed in the Y direction. The disc must be restricted to move in the global Y direction. The major load is acting on the disc is in ‘x’ direction for radial stresses and ‘z’ direction for hoop stress.

Coupling and constrain equations
In ANSYS there is an option called coupling and constrain equation to transfer the load to a structure from a remote distance or a remote point by creating a node.
Coupling and constraint equations allow you to relate the motion of one node to another. The coupling and constrain equation option is used to transfer the mechanical load from a remote point to the actual model. The effect of extra mass of mounted blades on the disc is given to the outer surface of the rim by placing a remote node, by which the effect of the blades to the outer rim of the disc is provided as shown in the fig 11. Thus the total overall loading effect of the blades is equally distributed on the outer rim surface area of the disc. To all the elements on the outer rim surface of the disc, the load of about 1500 KN/mm² is equally distributed. The chosen design parameters are the circuital design parameters of the disc. The chosen design parameters play a vital role in stress distribution pattern and mass reduction in the compressor disc. The chosen design parameters for shape optimization are “Bore inner radius”, “Bore width”, “Bore angle”, “Diaphragm width”.

Table: 6 Dimensional ranges chosen for optimization

<table>
<thead>
<tr>
<th>Variable Dimensional parameter</th>
<th>Dimensional range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bore inner radius</td>
<td>130 – 140 mm</td>
</tr>
<tr>
<td>Bore width</td>
<td>40 – 45 mm</td>
</tr>
<tr>
<td>Bore angle</td>
<td>35° – 45°</td>
</tr>
<tr>
<td>Diaphragm width</td>
<td>7 – 8 mm</td>
</tr>
</tbody>
</table>

Table: 7 Increments in the iteration

<table>
<thead>
<tr>
<th>Variable Dimensional parameter</th>
<th>Increment for case</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bore inner radius</td>
<td>10 mm</td>
</tr>
<tr>
<td>Bore width</td>
<td>5 mm</td>
</tr>
<tr>
<td>Bore angle</td>
<td>10°</td>
</tr>
<tr>
<td>Diaphragm width</td>
<td>2 mm</td>
</tr>
</tbody>
</table>

To give a jump for change in dimensions for the selected design parameters, the incremental values are provided. The incremental values given for the shape optimization are shown in the table7. The larger incremental values lesser cases for solving and lesser computational time. Smaller the incremental values more the number of cases and more the computational time. But due to the computational time factor, the incremental value was given to maximum difference of each variable dimensional parameter. Thus for every single case, one parameter is varied resulting in sixty four set of combinations for optimization process.

The results which were obtained in ANSYS 15 APDL were in the form of array parameters as shown in the result images in following case results. The GUI result viewing option for the parametric optimization is not available in ANSYS 15 APDL. Because of this reason the captured images are of the array parameters, which were inputted for optimization and they are shown in the output result images.
The variation of disc mass with respect to the number of cases in all the sixteen cases is as shown in the graph 6.1. Due to the reason that optimization of the compressor disc is done by changing the design parameters which constituted and forms the shape of the disc. The disc mass will be varied during all the cases during analysis, this gives us a chance for selecting the best possible result for optimization.

The graph in the graph 13 shows the variation of burst margin in all the case results. The shape of the disc varies constantly during optimization process due to the change in the element numbers in the disc in every case.
Table 8: Case results

<table>
<thead>
<tr>
<th>Case no.</th>
<th>Area weighted mean hoop stress</th>
<th>Limited area weighted mean hoop stress</th>
<th>Burst margin in %</th>
<th>Disc mass in KG</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>500.81 MPa</td>
<td>464 MPa</td>
<td>-0.0735</td>
<td>10.55</td>
</tr>
<tr>
<td>2</td>
<td>500.47 MPa</td>
<td>464 MPa</td>
<td>-0.07287</td>
<td>10.21</td>
</tr>
<tr>
<td>3</td>
<td>488 MPa</td>
<td>464 MPa</td>
<td>-0.04918</td>
<td>11.45</td>
</tr>
<tr>
<td>4</td>
<td>488.224 MPa</td>
<td>464 MPa</td>
<td>-0.04961</td>
<td>11.12</td>
</tr>
<tr>
<td>5</td>
<td>491.812 MPa</td>
<td>464 MPa</td>
<td>-0.05655</td>
<td>10.86</td>
</tr>
<tr>
<td>6</td>
<td>491.707 MPa</td>
<td>464 MPa</td>
<td>-0.05634</td>
<td>10.52</td>
</tr>
<tr>
<td>7</td>
<td>488.282 MPa</td>
<td>464 MPa</td>
<td>-0.04972</td>
<td>11.45</td>
</tr>
<tr>
<td>8</td>
<td>476.767 MPa</td>
<td>464 MPa</td>
<td>-0.02677</td>
<td>11.45</td>
</tr>
<tr>
<td>9</td>
<td>446.433 MPa</td>
<td>464 MPa</td>
<td>0.03934</td>
<td>12.13</td>
</tr>
<tr>
<td>10</td>
<td>442.903 MPa</td>
<td>464 MPa</td>
<td>0.04763</td>
<td>11.6</td>
</tr>
<tr>
<td>11</td>
<td>439.37 MPa</td>
<td>464 MPa</td>
<td>0.05605</td>
<td>12.84</td>
</tr>
<tr>
<td>12</td>
<td>435.92 MPa</td>
<td>464 MPa</td>
<td>0.06441</td>
<td>12.51</td>
</tr>
<tr>
<td>13</td>
<td>433.772 MPa</td>
<td>464 MPa</td>
<td>0.06968</td>
<td>12.42</td>
</tr>
<tr>
<td>14</td>
<td>431.66 MPa</td>
<td>464 MPa</td>
<td>0.07492</td>
<td>12.08</td>
</tr>
<tr>
<td>15</td>
<td>425.741 MPa</td>
<td>464 MPa</td>
<td>0.08986</td>
<td>13.36</td>
</tr>
<tr>
<td>16</td>
<td>423.855 MPa</td>
<td>464 MPa</td>
<td>0.09471</td>
<td>13.02</td>
</tr>
</tbody>
</table>

Optimization is the process of getting satisfied results by taking various design parameters into consideration. Finding an alternative with the most cost effective or highest achievable performance under the given constraints, by maximizing desired factors and minimizing undesired ones. In comparison, maximization means trying to attain the highest or maximum result or outcome without regard to cost or expense. Practice of optimization is restricted by the lack of full information, and the lack of time to evaluate what information is available (see bounded reality for details).

In computer simulation (modeling) of business problems, optimization is achieved usually by using linear programming techniques of operations research. In the current project weight reduction of compressor disc is the main objective. The compressor disc should be safe during the critical speed i.e. 125% of maximum rotational speed. The speed should be maintained during the critical working conditions at elevated temperatures. As a result, the optimum result which includes Design parameters like bore width, bore angle, bore inner radius and diaphragm width with better stress distribution patterns to the applied load exists in the design of the compressor disc.

Results for optimization
First optimum result
- Case no. 10

Table 9: results of Case 10

<table>
<thead>
<tr>
<th>Generated stress in MPa</th>
<th>Limited stress in MPa</th>
<th>Disk mass in KG</th>
<th>Increment in burst margin</th>
</tr>
</thead>
<tbody>
<tr>
<td>442.903</td>
<td>464</td>
<td>11.6</td>
<td>+0.04763</td>
</tr>
</tbody>
</table>

Second optimum result
- Case no. 14

Table 10: results of Case 14

<table>
<thead>
<tr>
<th>Generated stress in MPa</th>
<th>Limited stress in MPa</th>
<th>Disk mass in KG</th>
<th>Increment in burst margin</th>
</tr>
</thead>
<tbody>
<tr>
<td>431.66</td>
<td>464</td>
<td>12.08</td>
<td>+0.07492</td>
</tr>
</tbody>
</table>
The results for optimization are listed in two optimum results as shown in the above table. The shape optimization is done for the compressor disc for the provided dimensional ranges and material properties. The selection of the best results depends upon the weight reduction and safe design by increase in burst margin values, where the compressor disc can sustain few extra rpm along with critical speed safely without yielding.

IV. CONCLUSIONS AND SCOPE FOR FUTURE WORK

The shape optimization process is very handy in reducing the overall mass of the compressor disc, and the optimization for weight reduction and better efficiency can be carried out to other aircraft engine parts as well by FEA method. The process of optimization that is accomplished by FEA method reduces the costs by a great margin compared to the experimental work and also promotes for the future works. The sixteen cases give different results for carrying out optimization process of the compressor disc. These stress outputs obtained in the tool also matches the numerical calculations.

- The optimized results includes the verification of the safe design of the disc with sufficient burst margin increment, which in turn gives a few extra RPM above for the specified RPM for the critical speed.
- The disc can operate safely at a speed of 14005.5 rpm without yielding or getting fractured. Even at a given critical speed of 25% extra RPM than 14005.5 RPM the disc has a sufficient extra burst margin to operate.
- The first optimum result has a disc mass of 11.6 KG and +0.04763 extra margin and the second optimum result has a disc mass of 12.08 KG and +0.7492 extra burst margin than the specified critical speed.

Scope for the future work

- A thermal analysis featuring various temperature ranges and thermal stresses can be done.
- Dynamic analysis can be carried out in future.
- Fatigue analysis can be done to find endurance.
- The CFD analysis can be made by considering the fluid flow through airfoils and hot gases influence on the turbine blades can be considered.
- More steps by varying other design parameters can be made.

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