Complete X-ray Peak Profile Analysis of Co$_x$Zn$_{0.95-x}$Cr$_{0.05}$O nanoparticles based on Williamson–Hall and SSP Methods

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ABSTRACT: Co$_x$Zn$_{0.95-x}$Cr$_{0.05}$O nanoparticles of dilute magnetic semiconductor (DMS) were obtained by using sol-gel auto-combustion route. Powder X-ray diffraction technique was adopted to study the crystallography and strain mechanism induced in the crystal lattice. XRD patterns of all the samples confirm the single phase wurtzite type crystal structure without any impurity phase. Addition of isovalent transition metal Co$^{2+}$ ions in Zn-Cr crystal decreases the lattice parameter $a'$ and $c'$. Average crystallite and lattice strain induced in the crystal lattice was estimated by using the Williamson–Hall (W-H) and strain size plot (SSP) methods. Three different models Uniform deformation model (UDM), uniform stress deformation model (UDEM) and uniform deformation energy density model (UDEDM) were assumed for W-H analysis. Crystallite size obtained from another strain – size plot (SSP) method found in the range 19.32 to 25.60 nm and decreasing tensile type strain is induced in the crystal lattice which is in good agreement with the results obtained from W-H analysis.

KEYWORDS: Sol-gel synthesis, crystallite size, W-H analysis, strain size plot method

I. INTRODUCTION

Fabrications of nanostructured materials for particular application have attracted much attention of the researchers in the recent years. Nanomaterials show unusual physical and chemical properties over the bulk counterpart due to their large surface to volume ratio [1-3]. Dilute magnetic semiconductors (DMS), particularly transition metal doped zinc oxides are the subject of extensive research due to their fascinating structural, magnetic and optical properties [4]. Zinc oxide at room temperature possesses semiconducting behaviour with wide energy band gap (3.35 eV) and high excitation binding energy (60 meV) [2]. Semiconducting materials with improved optoelectronic properties, cost-effective and lightweight are gained prime importance and zinc oxide is one of the most useful materials. ZnO is one of the II-VI semiconducting materials possessing hexagonal wurtzite crystal geometry. Previous studies shows that the transition metal (TM) doped zinc oxide nanostructures have been comprehensively studied [5-9].

Synthesis routes and synthesis conditions and selection of proper dopant can control the physical properties of ZnO nanostructures such as shape and size of the material, magnetic, optical and electrical properties. Substitution of higher magnetic ion in ZnO lattice improves the magnetic behaviour of the doped samples. Based on desired applications, several synthesis routes have been developed in order to obtain the pure and doped ZnO nanoparticles which includes solvothermal, hydrothermal, sol-gel, sonochemical, chemical co-precipitation [10-12]. Among these, sol-gel synthesis route is one of the best methods to produce the DSM’s nanoparticles at large scale. This method has some advantages over the other synthesis approaches such as cost effective and relatively low temperature synthesis. Microstructural analysis is one of the most important properties of the nanomaterials which originate mainly due to the atomic
rearrangements in the crystal lattice after doping of other elements. These atomic rearrangements induce an intrinsic strain within the crystal lattice which in turn changes the microstructural properties. The substitution of TM ion in ZnO crystal lattice, due to its ionic radii difference, generates some defects within the crystal lattice which in turn influences the optical and magnetic properties [13-15]. Hence study of microstructural properties gets prime importance in order to understand the physical properties of ZnO nanoparticles. X-ray line broadening's clearly indicates the size and strain effect induced in the crystal lattice. X-ray peak profile analysis is one of the methods which provide the information of strain induced in the crystal lattice and other microstructural properties. Numerous methods have been developed to investigate the microstructural properties of nanoparticles by using X-ray peak profile analysis, such as Williamson-Hall (W-H), size – strain plot (SSP), Halder-Wagner (H-W), Nelson-Relay (N-R) etc [16-18].

In the present investigation, we have synthesized the Co$^{2+}$ doped Cr-Zn-O nanoparticles via sol-gel auto-combustion technique. All the samples were characterized by powder X-ray diffraction patterns. W-H and SSP methods have been adopted for the size and strain analysis of the samples by using X-ray line broadenings. Uniform deformation model (UDM), uniform stress deformation model (USDM) and uniform deformation energy density model were assumed for the W-H analysis and the results were compared with SSP method.

II. METHODOLOGY

Oxide nanoparticles of Co$_x$Zn$_{0.95-x}$Cr$_{0.05}$O ($x = 0.0, 0.02, 0.04, 0.06, 0.08$ and $0.1$) were produced by using sol-gel auto-ignition process. High purity (>98.5%) metal nitrates Co(NO$_3$)$_2$$\cdot$H$_2$O$_6$, Zn(NO$_3$)$_2$$\cdot$H$_2$O$_6$, Cr(NO$_3$)$_3$$\cdot$H$_2$O$_9$ and citric acid were used as raw materials. Deionized double distilled water was used to dissolve the raw materials with their weight proportion. The mixed solution was continuously stirred by maintaining the constant temperature of 90°C. Citric acid, as a chelating agent, was mixed in the nitrates solution with the ratio of 1:3 of metal nitrate to citrate. The pH of the solution was kept constant at 7 by slowly adding the liquid ammonia in the solution. Continuous stirring at constant pH and temperature for 2 to 3 hours converts the solution into viscous gel. After half an hour the dark brown gel was burnt by self-ignition process and converted into brown ash. The grinded ash powders were sintered at 900°C for 6 hours in order to obtain the final products. The as-prepare samples were characterized by X-ray diffraction technique for their structural investigations. Powder X-ray diffraction technique was adopted to obtain the XRD patterns at room temperature within the 2$\theta$ range of 20$^0$ to 80$^0$. All the XRD patterns were recorded on Regaku (Miniflux II) diffractometer with Cu-K$\alpha$ radiation (1.5406 Å) operated at 40 kV.

III. RESULTS AND DISCUSSION

![Fig. 1: X-ray diffraction patterns of Co$_x$Zn$_{0.95-x}$Cr$_{0.05}$O nanoparticles (left) and expanded (101) peak (right)](image)

Powder X-ray diffraction patterns of Co$_x$Zn$_{0.95-x}$Cr$_{0.05}$O ($x = 0.0, 0.02, 0.04, 0.06, 0.08$ and $0.1$) recorded at room temperature are given in Figure 1 (Left panel). Bragg’s reflections occurred for the planes (100), (002), (101), (102), (110), (103), (200), (112), (201), (004), and (202) confirm the hexagonal wurtzite structure corresponding to the space group P6$_3$mc. No any un-indexed reflection peak is observed which implies that all the samples possesses single phase. Right panel of Figure 1 shows the expanded view of most intensive plane (101) which clearly shows that peak height decreases and peak position shifted slightly towards higher angles with the addition of Co$^{2+}$ ions in Cr-Zn crystal lattice. Shifting of peak position towards higher angles directly affects the lattice parameter of the samples which in turn decreases with Co$^{2+}$ addition.
and the values are listed in Table 1. Decrease in lattice parameters shrinks the 

$$ b_x (4)$$

slope of UDM plots gives the 

seen from Table 2 that the average crystallite size obtained from UDM plots varies from 19.36 to 25.63 nm with the 

lattice strain induced in the crystal lattice whereas Y-intercept gives the value of average crystallite size (t). It can be 

Figure 2 shows the linearly fitted UDM plots drawn between 

$$ x = 0.06$$

$$ x = 0.08$$

$$ x = 0.1$$

Lattice constants ‘a’ and ‘c’ for hexagonal crystal geometry were evaluated by using the relations discussed elsewhere [19] which are given in Table 1. Addition of Co$^{2+}$ ions in Cr-Zn-O crystal lattice reduces the lattice parameter ‘a’ from 3.2487 to 3.2478 Å and ‘c’ from 5.2043 to 5.2035 Å. The decrease in lattice parameter is strongly related to the ionic radii difference of Co$^{2+}$ and Zn$^{2+}$. Here in the present case, Co$^{2+}$ ions having ionic radii (0.74Å) replaces the Zn$^{2+}$ ions having relatively larger ionic radii (0.83Å) which in turn shrinks the lattice lengths. The constant value of c/a ratio (1.602) for all the samples confirms the hexagonal crystal geometry of the samples. Unit cell volume of the samples was estimated by using 

$$ V = 0.866 a^2 c$$

and the values are listed in Table 1. Decrease in lattice parameters shrinks the cell volume from 47.599 to 47.567 Å$^3$ indicating that the Co$^{2+}$ ions are successfully incorporated in the crystal lattice. The distortion factor ‘u’ for the wurtzite structure was calculated by using the following relation [20]:

$$ u = \frac{a^2}{3c^2} + 0.25$$

As explained by Bindu et al. [21], distortion factor ‘u’ is estimation of the displacement of each atom along ‘c’ axis with respect to next atom. The estimated value of ‘u’ (0.379) for each sample is very close to the standard value (0.375) [20]. Mass – volume relation was used to estimate the bulk density and X-ray density was calculated by using the relation taken from literature [22]. Percentage porosity and specific surface area of all the samples were obtained by using the following relations [22]:

$$ P(\%) = \left( \frac{d_x - d_B}{d_B} \right) \times 100$$

$$ S = \frac{6000}{d_B}$$

Where, $d_x$ is the X-ray density, $d_B$ – bulk density, $S$ – specific surface area, $t$ – is crystallite size and $d_B$ is the bulk density. Calculated values of X-ray density, porosity and specific surface area are listed in Table 1. It can be seen that the X-ray density and percentage porosity increases while as specific surface area decreases with the addition Co$^{2+}$ ions in Cr-Zn crystal lattice. The XRD peak broadenings were analyzed by using W-H analysis which provides the information of size and shape of the samples. Crystalite size and lattice strain induced in the crystal lattice were computed by using the following equation which assumes the uniform deformation model (UDM) [23]:

$$ \beta \cos \theta = 4e \sin \theta + \frac{k\lambda}{l \text{W-H}}$$

Figure 2 shows the linearly fitted UDM plots drawn between $4\sin \theta$ and $\beta \cos \theta$. Slopes of UDM plots gives the lattice strain induced in the crystal lattice whereas Y-intercept gives the value of average crystallite size (t). It can be seen from Table 2 that the average crystallite size obtained from UDM plots varies from 19.36 to 25.63 nm with the addition of Co$^{2+}$ ions. While as, positive values of lattice strain induced in the crystal lattice indicating the tensile type of strain which reduces from $2.35 \times 10^{-4}$ to $0.619 \times 10^{-4}$ with the addition of Co$^{2+}$ ions.

<table>
<thead>
<tr>
<th>'X'</th>
<th>Lattice parameter (Å)</th>
<th>'V' (Å$^3$)</th>
<th>'u'</th>
<th>'d_X' (gm/cc)</th>
<th>'P' (%)</th>
<th>'S' (m$^2$/gm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0</td>
<td>3.2487</td>
<td>5.2043</td>
<td>1.602</td>
<td>47.599</td>
<td>0.379</td>
<td>5.635</td>
</tr>
<tr>
<td>0.02</td>
<td>3.2486</td>
<td>5.2042</td>
<td>1.602</td>
<td>47.595</td>
<td>0.379</td>
<td>5.627</td>
</tr>
<tr>
<td>0.04</td>
<td>3.2485</td>
<td>5.2041</td>
<td>1.602</td>
<td>47.591</td>
<td>0.379</td>
<td>5.618</td>
</tr>
<tr>
<td>0.06</td>
<td>3.2483</td>
<td>5.2040</td>
<td>1.602</td>
<td>47.586</td>
<td>0.379</td>
<td>5.610</td>
</tr>
<tr>
<td>0.08</td>
<td>3.2481</td>
<td>5.2038</td>
<td>1.602</td>
<td>47.579</td>
<td>0.379</td>
<td>5.601</td>
</tr>
<tr>
<td>0.1</td>
<td>3.2478</td>
<td>5.2035</td>
<td>1.602</td>
<td>47.567</td>
<td>0.379</td>
<td>5.594</td>
</tr>
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</table>
Microstructure of the materials has prime importance in accordance with the electrical and magnetic properties. Equation (4) is based on the isotropic nature of the samples and uniform strain induced in the crystal lattice. Uniform stress deformation model (USDM), is the another deformation model considered for the evaluation of strain and crystallite size.

![Fig. 2: W-H plots of Uniform Deformation Model for Co$_x$Zn$_{0.95-x}$Cr$_{0.05}$O nanoparticles](image)

**Table 2: Crystallite size (t) and strain induced in Co$_x$Zn$_{0.95-x}$Cr$_{0.05}$O**

<table>
<thead>
<tr>
<th>‘x’</th>
<th>UDM</th>
<th>USDM</th>
<th>UDEDM</th>
<th>SSP Method</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>‘t’ (nm)</td>
<td>$\varepsilon_x 10^4$</td>
<td>‘t’ (nm)</td>
<td>$\varepsilon_x 10^4$</td>
</tr>
<tr>
<td>0.0</td>
<td>19.36</td>
<td>2.35</td>
<td>19.28</td>
<td>2.20</td>
</tr>
<tr>
<td>0.02</td>
<td>20.40</td>
<td>1.65</td>
<td>20.37</td>
<td>1.55</td>
</tr>
<tr>
<td>0.04</td>
<td>21.23</td>
<td>0.937</td>
<td>21.20</td>
<td>0.864</td>
</tr>
<tr>
<td>0.06</td>
<td>22.56</td>
<td>0.808</td>
<td>22.28</td>
<td>0.735</td>
</tr>
<tr>
<td>0.08</td>
<td>23.74</td>
<td>0.716</td>
<td>24.13</td>
<td>0.662</td>
</tr>
<tr>
<td>1.0</td>
<td>25.63</td>
<td>0.619</td>
<td>25.58</td>
<td>0.572</td>
</tr>
</tbody>
</table>

Figure 3 shows the USDM plots drawn between $\beta \cos \theta$ and $4 \sin \theta / Y_{hkl}$ obtained by applying the Hook’s law. There is linear relationship between stress and strain induced in the crystal lattice and is given by $\varepsilon = \sigma / Y$, where $\sigma$ - is stress and Y is Young’s modulus. Hook’s law modified the equation (4) as:

$$\beta \cos \theta = \sigma \left(\frac{4 \sin \theta}{Y_{hkl}}\right) + \frac{k \lambda}{t_{W-H}}$$

(5)
Young’s modulus $Y_{hkl}$ is obtained from the following relation [24]:

$$
Y_{hkl} = \frac{\left[ h^2 + \left( \frac{2k}{3} + \frac{1}{c} \right)^2 \right]^2}{S_{11} \left( h^2 + \frac{(h+2k)^2}{3} \right) + S_{33} \left( \frac{a}{c} \right)^4 + (2S_{13} + S_{44}) \left( h^2 + \frac{(h+2k)^2}{3} \right) \left( \frac{a}{c} \right)^2}
$$

(6)

Stress induced in the crystal lattice was obtained from the slope of linearly fitted USDM plots shown in Figure 3 and the Y-intercept gives the values of average crystallite size of the samples. Table 2 represents the stress, strain and crystallite size obtained from USDM plots.

Figure 4, represents the UDEDM plots drawn between $\cos \beta \theta$ and $\frac{4 \text{Sin} \theta}{Y_{hkl} / 2}$. Slope of the plots gives the root mean square values of energy density from which strain can be calculated and Y-intercept gives the values of crystallite size $t_{W-H}$. Both lattice strain and average crystallite size obtained from all the three models viz. UDM, USD, and UDEDM are in good agreement with each other.

W-H analysis is completely true when the line broadening is essentially isotropic which implies that the strain induced within the crystal lattice is uniformly distributed. Another method, size-strain plot method, which evaluates the size and strain by considering Lorentzian and Gaussian functions for X-ray line profile fitting [25].

$$
\left( \frac{d \beta \cos \theta}{2} \right)^2 = \left( \frac{a}{2} \right)^2 + \frac{k \lambda}{t_{W-H}} \left( d^2 \beta \cos \theta \right)
$$

(8)
Figure 5 shows the size-strain plots drawn between $(\frac{d\beta}{d\theta})^2$ and $d^2\beta d\theta$. Crystallite size and lattice strain obtained from the slopes and Y-intercept of strain-size plots are given in Table 2, which are in good agreement with the W-H analysis.

**IV. CONCLUSIONS**

Oxide nanoparticles of Co$^{2+}$ doped Cr-Zn-O were successfully obtained by using the sol-gel auto-ignition route. Single phase hexagonal wurtzite crystal structure of all the samples was confirmed by using X-ray diffraction analysis. Bragg’s peak positions shifted slightly towards higher angles which decreases lattice constants ‘a’ and ‘c’ with the substitution of Co$^{2+}$ ions in Cr-Zn crystal lattice. W-H analysis and SSP method indicate that the tensile type strain is induced in the crystal lattice and it decreases with the increasing percentage of Co$^{2+}$ ions. Crystallite size obtained from both W-H and SSP methods is obtained in nanometer range. Lattice strain induced in the crystal lattice obtained from SSP method ranges from $6.49 \times 10^{-3}$ to $2.69 \times 10^{-3}$ and its variation is in good agreement with the results obtained from W-H analysis.

**REFERENCES**


[14] S. R. Wadgane, S. T. Alone, A. Karim, G. Vats, S. E. Shirsath, R. H. Kadam; Magnetic field induced polarization and magneto-electric effect in Na0.5Bi0.5TiO3-Co0.25Zn0.25Cr0.5Fe1.5O4; J. Magn. Magn. Mater. vol. 471, pp. 388-393, 2019.


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