

# Generation Fuel Cost Minimization of Power Grid Using Primal Dual Interior Point OPF (Optimal Power Flow) Method

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**Abstract:** This paper presents an efficient and reliable interior point approach to obtain optimal power flow (OPF) problem solution. The Interior Point method (IP) is found to be the most efficient algorithm for optimal power flow solution. The IP algorithm is coded in MATLAB and the performance is tested on IEEE 14 bus test system with fuel cost minimization as objective function. It maintains good accuracy while achieving the high speed of convergence when compared to other known linear programming methods. The solution obtained by this algorithm proves to be robust to solve the OPF problem of power grid.

**Keywords:** Interior point method, optimal power flow, optimization techniques, cost minimization, power grid, MATLAB.

## I. INTRODUCTION

Present day commercial OPF programs can solve very large and complex power systems optimization problems in a relatively less time. Many different solution methods have been suggested to solve OPF problems. In a conventional power flow, the values of the control variables are predetermined. In an OPF, the values of some or all of the control variables need to be known so as to optimize (minimize or maximize) a predefined objective. The OPF calculation has many applications in power systems, real-time control, operational planning, long-term planning and energy management systems (EMSs) [1–2]. OPF continues to be significant due to the growth in power system size and complex interconnections [3 – 4]. For example, OPF should support deregulation transactions or furnish information on what reinforcement is required. OPF studies can decide the tradeoffs between reinforcements and control options as per the results obtained from carrying out OPF studies. It is clarified when a control option enhances utilization of an existing asset (e.g., generation or transmission), or when a control option is an inexpensive alternative to installing new facilities. Issues of priority of transmission access and VAR pricing or auxiliary costing to afford price and purchases can be done by OPF.

The main goal of a generic OPF is to reduce the costs of meeting the load demand for a power system while up keeping the security of the system. From the viewpoint of an OPF, the maintenance of system security requires keeping each device in the power system within its desired operation range at steady-state. This will include maximum and minimum outputs for generators, maximum MVA flows on transmission lines and transformers, as well as keeping system bus voltages within specified ranges.

The secondary goal of an OPF is the determination of system marginal cost data. This marginal cost data can aid in the pricing of MW transactions as well as the pricing auxiliary services such as voltage support through MVAR support. The OPF is capable of performing all of the control functions necessary for the power system. While the economic dispatch of a power system does control generator MW output, the OPF controls transformer tap ratios and phase shift

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angles as well. The OPF also is able to monitor system security issues including line overloads and low or high voltage problems. If any security problems occur, the OPF will modify its controls to fix them, i.e., remove a transmission line overload [13].

The quality of the solution depends on the accuracy of the model used. It is essential to define problem properly with clearly stated objectives be given at the onset. No two-power system utilities have the same type of devices and operating requirements. The model form presented here allows OPF development to easily customize its solution to different cases under study [5–8].

OPF, to a large extent depends on static optimization method for minimizing a scalar optimization function (e.g., cost). It was first introduced in the 1960s by Tinney and Dommel [3]. It employs first-order gradient algorithm for minimization objective function subject to equality and inequality constraints. Solution methods were not popular as they are computationally intensive than traditional power flow. The next generation OPF has been complex as power systems operation or planning need to know the limit, the cost of power, incentive for adding units, and building transmission systems a particular load entity.

## II. OPTIMAL POWER FLOW CHALLENGES

The demand for an OPF tool has been increasing to assess the state and recommended control actions both for off line and online studies, since the first OPF paper was presented in 60's. The thrust for OPF to solve problems of today's deregulated industry and the unsolved problem in the vertically integrated industry has posed further challenges to OPF to evaluate the capabilities of existing OPF in terms of its potential and abilities [9].

Many challenges are before OPF remain to be answered. They can be listed as given below.

1. Because of the consideration of large number of variety of constraints and due to non linearity of mathematical models OPF poses a big challenge for the mathematicians as well as for engineers in obtaining optimum solutions.
  2. The deregulated electricity market seeks answer from OPF, to address a variety of different types of market participants, data model requirements and real time processing and selection of appropriate costing for each unbundled service evaluation.
  3. To cope up with response time requirements, modelling of externalities (loop flow, environmental and simultaneous transfers), practicality and sensitivity for on line use.
  4. How well the future OPF provide local or global control measures to support the impact of critical contingencies, which threaten system voltage and angle stability simulated.
  5. Future OPF has to address the gamut of operation and planning environment in providing new generation facilities, unbundled transmission services and other resources allocations.
- Finally it has to be simple to use and portable and fast enough.

## III. OPTIMAL POWER FLOW PROBLEM

In an OPF, the values of some or all of the control variables need to be found so as to optimise (minimise or maximize) a predefined objective. It is also important that the proper problem definition with clearly stated objectives be given at the onset. The quality of the solution depends on the accuracy of the model studied. Objectives must be modelled and its practicality with possible solutions.

Objective function takes various forms such as fuel cost, transmission losses and reactive source allocation. Usually the objective function of interest is the minimisation of total production cost of scheduled generating units. This is most used as it reflects current economic dispatch practice and importantly cost related aspect is always ranked high among operational requirements in power systems [15].

OPF aims to optimise a certain objective, subject to the network power flow equations and system and equipment operating limits. The optimal condition is attained by adjusting the available controls to minimise an objective function subject to specified operating and security requirements.

Some well-known objectives can be identified as below:

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## Active power objectives

1. Economic dispatch (minimum cost, losses, MW generation or transmission losses)
2. Environmental dispatch
3. Maximum power transfer

## Reactive power objectives

MW and MVar loss minimization

## General goals

1. Minimum deviation from a target schedule
2. Minimum control shifts to alleviate Violations
3. Least absolute shift approximation of control shift

Among the above the following objectives are most commonly used:

- (a) Fuel or active power cost optimisation
- (b) Active power loss minimisation
- (c) VAr planning to minimise the cost of reactive power support

The mathematical description of the OPF problem is presented below:

## OPF Objective Function for Fuel Cost Minimization

The OPF problem can be formulated as an optimization problem [10] and is as follows:

Total Generation cost function is expressed as:

$$F(P_G) = \sum_{i=1}^{N_G} (\alpha_i + \beta_i P_{G_i} + \gamma_i P_{G_i}^2) \quad (1)$$

The objective function is expressed as:

$$\text{Min } F(P_G) = f(x, u) \quad (2)$$

Subject to satisfaction of Non linear Equality constraints:

$$g(x, u) = 0 \quad (3)$$

and Non Linear Inequality constraints:

$$h(x, u) \leq 0 \quad (4)$$

$$u^{\min} \leq u \leq u^{\max} \quad (5)$$

$$x^{\min} \leq x \leq x^{\max} \quad (6)$$

$F(P_G)$  is total cost function  $f(x, u)$  is the scalar objective,  $g(x, u) = 0$  represents nonlinear equality constraints (power flow equations), and  $h(x, u)$  is the nonlinear inequality constraint of vector arguments  $x, u$ .

The vector  $x$  contains dependent variables consisting of:

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- Bus voltage magnitudes and phase angles
- MVAR output of generators designated for bus voltage control
- Fixed parameters such as the reference bus angle
- Non controlled generator MW and MVAR outputs
- Non controlled MW and MVAR loads
- Fixed bus voltages, line parameters

The vector  $u$  consists of control variables including:

- Real and reactive power generation
- Phase – shifter angles
- Net interchange
- Load MW and MVAR (load shedding)
- DC transmission line flows
- Control voltage settings
- LTC transformer tap settings

The equality and inequality constraints are:

- Limits on all control variables
- Power flow equations
- Generation / load balance
- Branch flow limits (MW, MVAR, MVA)
- Bus voltage limits
- Active / reactive reserve limits
- Generator MVAR limits
- Corridor (transmission interface) limits

### Constraints for Objective Function of Fuel Cost Minimization

The network equality constraints are represented by the load flow equations

$$P_i(V, \delta) - P_{Gi} + P_{Di} = 0 \quad (7)$$

$$Q_i(V, \delta) - Q_{Gi} + Q_{Di} = 0 \quad (8)$$

Where:

$$P_i(V, \delta) = |V_i| \sum_{j=1}^N |V_j| |Y_{ij}| \cos(\delta_i - \delta_j - \phi_{ij}) \quad (9)$$

$$Q_i(V, \delta) = |V_i| \sum_{j=1}^N |V_j| |Y_{ij}| \sin(\delta_i - \delta_j - \phi_{ij}) \quad (10)$$

$$Y_{ij} = |Y_{ij}| \angle \phi_{ij} \quad (11)$$

and load balance equation:

$$\sum_{i=1}^{N_G} (P_{Gi}) - \sum_{i=1}^{N_D} (P_{Di}) - P_L = 0 \quad (12)$$

The Inequality constraints representing the limits on all variables, line flow constraints are as:

$$V_{i \min} \leq V_i \leq V_{i \max}, \quad i=1, 2, \dots, N \quad (13)$$

$$P_{G_i \min} \leq P_{G_i} \leq P_{G_i \max}, \quad i=1, 2, \dots, N_G \quad (14)$$

$$Q_{G_i \min} \leq Q_{G_i} \leq Q_{G_i \max}, \quad i=1, 2, \dots, N_{G_q} \quad (15)$$

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$$-K_{vi}I_{lmax} \leq V_i - V_j \leq K_{vj}I_{lmax}, i=1,2,\dots,N_l \quad (16) \quad \text{Where } i, j \text{ are the nodes of line } l$$

$$-K_{\delta i}I_{lmax} \leq \delta_i - \delta_j \leq K_{\delta j}I_{lmax}, i=1,2,\dots,N_l \quad (17) \quad \text{Where } i, j \text{ are the nodes of line } l$$

$$S_{l_i} \leq S_{l_{max}} \quad i=1,2,\dots,N_l \quad (18)$$

$$T_{k \min} \leq T_k \leq T_{k \max} \quad i=1,2,\dots,N_l \quad (19)$$

$$\delta_{i \min} \leq \delta_i \leq \delta_{i \max} \quad i=1,2,\dots,N_l \quad (20)$$

## IV. INTERIOR POINT METHOD

It has been found that, the projective scaling algorithm for linear programming proposed by N. Karmarkar is characterized by significant speed advantages for large problems reported to be as much as 12:1 when compared to the simplex method. Further, this method has a polynomial bound on worst-case running time that is better than the ellipsoid algorithms. Karmarkar’s algorithm is significantly different from Dantzig’s simplex method. Karmarkar’s interior point rarely visits too many extreme points before an optimal point is found. In addition, the IP method stays in the interior of the polytope and tries to position a current solution as the “center of the universe” in finding a better direction for the next move. By properly choosing the step lengths, an optimal solution is achieved after a number of iterations. Although this IP approach requires more computational time in finding a moving direction than the traditional simplex method, better moving direction is achieved resulting in less iteration. In this way, the IP approach has become a major rival of the simplex method and has attracted attention in the optimization community. The Interior Point Method [10] is one of the most efficient algorithms. The IP method classification is a relatively new optimization approach that was applied to solve power system optimization problems in the late 1980s and early 1990s and as can be seen from the list of references [11]. The Interior Point Method (IPM) can solve a large scale linear programming problem by moving through the interior, rather than the boundary as in the simplex method, of the feasible region to find an optimal solution. The IP method was originally proposed to solve linear programming problems; however later it was implemented to efficiently handle quadratic programming problems. It is known as an interior method, since it finds improved search directions strictly in the interior of the feasible space as shown in Fig.1.

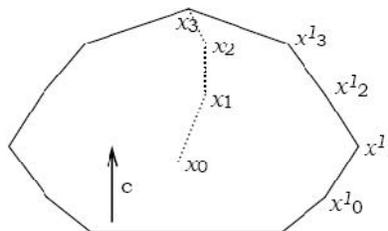


Fig.1. Polytope of a two – dimension feasible region.

The basic ideas involved in the iteration process of Interior Point Method as proposed by N. K.Karmarkar [12], are given below. In order to have a comprehensive idea of the optimisation process, the difference between the simplex and interior point methods is described geometrically. Consider an interior path, described by  $x_i$ , as shown in Fig.1. In the simplex method the solution goes from corner point to corner point, as indicated by  $x_i$ . The steepest descent direction is represented by  $c$ . The main features of the IPM as shown in Fig.1 are:

- 1) Starting from an interior point, the method constructs a path that reaches the optimal solution after little iteration (less than the simplex method).
- 2) The IPM leads to a “good assessment” of the optimal solution after the first few iterations. This feature is very important, because for each linearization of the original formulation an exact result of Quadratic Programming problem is not imperative. Normally it is enough to obtain a point near the optimal solution because each QP sub problem is already an approximation of the original problem.

The interior point method starts by determining an initial solution using Mehrotra’s algorithm, to locate a feasible or near-feasible solution. There are two procedures to be performed in an iterative manner until the optimal solution has

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been found. The formal is the determination of a search direction for each variable in the search space by a Newton's method. The lateral is the determination of a step length normally assigned a value as close to unity as possible to accelerate solution convergence while strictly maintaining primal and dual feasibility. A calculated solution in each iteration to be checked for optimality by the Karush – Kuhn – Tucker (KKT) conditions, which consist of primal feasibility, dual feasibility and complementary slackness.

### OPF Problem Formulation by Primal — Dual Interior Point Method

As has been mentioned, the objective function considered in this paper is to minimize the total production cost of scheduled generating units. OPF formulation consists of three main components: objective function, equality constraints, and inequality constraints [16-17].

An OPF problem is generally formulated as per Eq. (1) – (6).

#### Objective Function

The objective function is given by Eq. (2) and is reproduced below.

$$F(P_G) = \sum_{i=1}^{N_G} (\alpha_i + \beta_i P_{G_i} + \gamma_i P_{G_i}^2)$$

#### Equality Constraints

The equality constraints are active/reactive power flow equations.

Nonlinear equations can be linearized by the Taylor's expansion using

$$\begin{pmatrix} \Delta P(V, \delta) \\ \Delta Q(V, \delta) \end{pmatrix} = \begin{pmatrix} J_{11} & J_{12} \\ J_{21} & J_{22} \end{pmatrix} \begin{pmatrix} \Delta \delta \\ \Delta V \end{pmatrix}$$

Where  $\begin{pmatrix} J_{11} & J_{12} \\ J_{21} & J_{22} \end{pmatrix}$  is the Jacobian matrix.

Transmission loss (PL) can be directly calculated from the power flow.

#### Inequality Constraints

The inequality constraints consist of generator active/reactive power limits, voltage magnitude limits, and transformer tap position limits.

### Solution Algorithm

The PDIPM method is started by arranging a primal quadratic programming problem into a standard form as:

$$\text{Minimize } \frac{1}{2} x^T Q x + c^T x \quad (21)$$

$$\text{Subject to } Ax = b, x \geq 0 \quad (22)$$

Eq. (21) can be transformed into the corresponding dual problem having the form.

Maximize

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$$-\frac{1}{2}x^T Qx + b^T W \quad (23)$$

Subject to  $-Qx + A^T w + s = c$ ,

$$s \geq 0 \quad (24)$$

$$Ax = b, x \geq 0 \text{ (Primal feasibility)} \quad (25)$$

$$-Qx + A^T w + s = c, s \geq 0 \text{ (Dual feasibility)} \quad (26)$$

$$XSe = \mu e \text{ (Complementary Slackness)} \quad (27)$$

Where

$$\mu^k = \frac{(x^k)^T s^k}{n} \quad (28)$$

From the KKT conditions Eq. (25-27), the directions of translation are calculated using the Newton's method which yields the following system Eq.

$$\begin{bmatrix} A & 0 & 0 \\ -Q & A^T & I \\ S^k & 0 & X^k \end{bmatrix} \begin{bmatrix} d_x^k \\ d_w^k \\ d_s^k \end{bmatrix} = \begin{bmatrix} Ax^k - b \\ -Qx^k + A^T w^k + s^k - c \\ X^k S^k e - \mu^k e \end{bmatrix} \quad (29)$$

The right hand side of Eq. (29) is so-called slackness vectors and can be assigned to new variables as

$$t^k = b - Ax^k \quad (30)$$

$$u^k = Qx^k + c - A^T w^k - s^k \quad (31)$$

$$v^k = \mu^k e - X^k S^k e \quad (32)$$

From Eq. (29) – (32), we have

$$A d_x^k = t^k \quad (33)$$

$$-Q d_x^k + A^T d_w^k + d_s^k = u^k \quad (34)$$

$$S_k d_x^k + X_k d_s^k = v^k \quad (35)$$

Combining and rearranging Eq. (34) and Eq. (35) gives

$$-d_x^k + (S_k + X_k Q)^{-1} X_k A^T d_w^k = (S_k + X_k Q)^{-1} (X_k u^k - v^k) \quad (36)$$

With Eq. (33) and Eq. (36), a dual search direction can be derived a

$$d_w^k = [A(S_k + X_k Q)^{-1} X_k A^T]^{-1} - [A(S_k + X_k Q)^{-1} (X_k u^k - v^k) + t^k] \quad (37)$$

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The equation for a primal search direction can be derived from Eq. (36).

$$d_x^k = (S_k + X_k Q)^{-1} [X_k (A^T d_w^k - u^k) + v^k] \quad (38)$$

With the primal search direction and Eq. (35), a slack search direction can be obtained by

$$d_s^k = X_k^{-1} (v^k - S_k d_x^k) \quad (39)$$

To find appropriate step lengths while keeping the primal and dual problem feasible, Eq. (40) – Eq. (43) are used.

$$\alpha_p^k = \min \left( -\frac{x_j^k}{d_{x_j}^k} \right) | d_{x_j}^k < 0 \quad (40)$$

$$\alpha_D^k = \min \left( -\frac{s_j^k}{d_{s_j}^k} \right) | d_{s_j}^k < 0 \quad (41)$$

$$\alpha_{max}^k = \min(\alpha_p^k, \alpha_D^k) \quad (42)$$

$$\alpha^k = 0.99 \alpha_{max}^k \quad (43)$$

An updated solution can be computed by Eq. (44) – (46).

$$x^{k+1} = x^k + \alpha^k d_x^k \quad (44)$$

$$w^{k+1} = w^k + \alpha^k d_w^k \quad (45)$$

$$S^{k+1} = S^k + \alpha^k d_s^k \quad (46)$$

### Algorithm for PDIPM

The PDIPM algorithm applied to the OPF problem is summarized step-by-step as follows.

**Step 1:** Read relevant input data.

**Step 2:** Perform a base case power flow by a power flow subroutine.

**Step 3:** Establish an OPF model.

**Step 4:** Compute Eq. (30) – (32).

**Step 5:** Calculate search directions with Eq. (37) – (39).

**Step 6:** Compute primal, dual and actual step-lengths with Eq. (40) – (43).

**Step 7:** Update the solution vectors with Eq. (44) – (46).

**Step 8:** Check if the optimality conditions are satisfied by Eq. (25) – (27) and if  $\mu \leq \epsilon$  ( $\epsilon = 0.001$  is chosen).

If yes, go to the next step. Otherwise go to step 4.

**Step 9:** Perform the power flow subroutine.

**Step 10:** Check if there are any violations in Eq. (15) and Eq. (19). If no, go to the next step; otherwise, go to step 4.

**Step 11:** Check if a change in the objective function is less than or equal to the prespecified tolerance. If yes, go to the next step; otherwise, go to step 4.

**Step 12:** Print and display an optimal power flow solution.

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### V. OPF TEST CASE: - IEEE 14 BUS TEST SYSTEM

In this study, the standard IEEE 14-Bus 5 Generator test system is considered to investigate effectiveness of the proposed method. The IEEE 14-bus system has 20 transmission lines [14]. The single line diagram is shown in Fig.2.

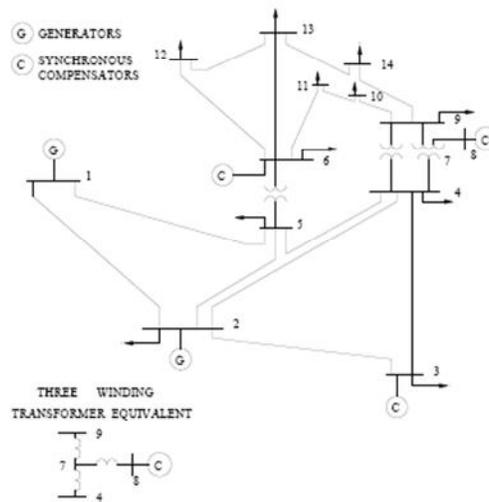


Fig. 2. IEEE 14-Bus test System

The values of fuel cost coefficients are given in Table 1. The total load demand of the system is 259 MW and 5 - Generators should share load optimally.

**Table 1: Generator Fuel Cost Coefficients**

Sl.No	Generator at bus #	$\alpha_i$ (\$/h)	$\beta_i$ (\$/MWhr)	$\gamma_i$ (\$/MWhr <sup>2</sup> )
1	1	0	20	0.0430293
2	2	0	20	0.25
3	3	0	40	0.01
4	6	0	40	0.01
5	8	0	40	0.01

(Minimum or Maximum Generation limits of Generators are presented in Table 2)

**Table 2: Generation limits of Generators**

Sl.No	Generator at bus #	$P_{Gr}^{Min}$ (MW)	$P_{Gr}^{Max}$ (MW)
1	1	0	332.4
2	2	0	140
3	3	0	100
4	6	0	100
5	8	0	100

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## VI. OPF RESULTS

CPU Computational Time= 0.29 seconds

Total Generation Cost = 8081.53 \$/hr

**Table 3.1 OPF Solution: Generation Schedule**

Parameter	OPF Solution by IP Method (MW)
$P_{G1}$	194.33
$P_{G2}$	36.72
$P_{G3}$	28.74
$P_{G6}$	11.20
$P_{G8}$	8.50

**Table 3.2 Voltage Magnitude and Incremental Costs at Different Buses.**

Bus No.	Voltage at different Buses (in p.u)	Bus Incremental Costs	
		Lambda P(\$/MW-hr)	Lambda Q(\$/MVAR-hr)
1	1.060	36.724	-0.094
2	1.041	38.360	-
3	1.016	40.575	-
4	1.014	40.190	0.120
5	1.016	39.661	0.208
6	1.060	39.734	-
7	1.046	40.172	0.120
8	1.060	40.170	-
9	1.044	40.166	0.196
10	1.039	40.318	0.309
11	1.046	40.155	0.228
12	1.045	40.379	0.212
13	1.040	40.575	0.353
14	1.024	41.198	0.571

## VII. CONCLUSION

In this paper, primal dual interior point algorithm(PDIP) is used to solve the optimal power flow problem in power systems. The OPF problem is formulated as a linear optimization problem with equality and inequality constraints in power systems. The minimization of fuel cost is considered as objective function. This approach was successfully and influentially performed to find the optimal settings of the control variables of test system(IEEE 14 bus). The simulation results proved the robustness of the PD interior point method to solve the OPF problem. The effectiveness of this algorithm is demonstrated on IEEE 14 bus system.

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