

Control of a Nonlinear Spherical Tank Process Using GA Tuned PID Controller

D.Pradeepkannan, Dr.S.Sathiyamoorthy

Department of Electronics and Instrumentation, K. L. N. College of Engineering, Pottapalayam, India

Department of Electronics and Instrumentation, J.J. College of Engineering and Technology, Tiruchirappalli, India.

ABSTRACT— *Conventional PID controller is a simplest well known controller used in almost all process Industries for controlling the process parameters at desired set value. The tuning of these controllers is done by a classical Zeigler Nichols (ZN) tuning. The dynamics of a spherical tank process is nonlinear in nature and it exhibits non linear behavior and time delays between the inputs and outputs. The ZN tuned PID controller parameters does not cope with all operating points as it exhibits different non linear characteristics at various operating points. This paper aims at real time implementation of enhanced PID controller performance for a nonlinear spherical tank process. The idea is to keep the ZN tuned PID values as the base value so as to fine tune these parameters using a Genetic Algorithm approach to obtain the optimal set of tuning values which can cope up with all operating points. The mathematical model is developed by applying the governing mass balance equations and substituting the arbitrary constants. The system identification of the non linear process is done by black box modeling and found to be (FOPDT) First order plus dead time model. The controller performance of the ZN tuned PID controller is fine tuned using GA based PID controller in terms of time domain specification as well as performance indices. Better enhanced controller performance was obtained for a GA tuned PID controller than that of ZN tuned PID controller at all operating points. All the simulations are carried out in Mat lab environment and the real time implementation is done on a single spherical tank setup in LabVIEW Environment.*

KEYWORDS— PID controller; ZN tuning; Genetic Algorithm; Non linear spherical tank process.

I. INTRODUCTION

Proportional Integral Derivative Controller has been using in Industrial control applications for a long time. The reasons for their wide popularity lies in the simplicity of design and good performance which includes low percent over shoot and small settling time for slow process *Astrom.K.J and Hagglund.T,(1995)*.According to the survey in 1989, 90 percentage of process industries uses the conventional PID controllers [3].The wide spread use of the PID controller in the Industry is due to their simplicity and ease of retuning online [4].The PID controller is so named because its output sum of three terms, proportional, integral and derivative term. Each of these terms is dependent on the error value 'e' between the input and the output.

$$u(t) = K_c [e(t) + \frac{1}{\tau_i} \int_0^t e(t) dt + \tau_d \frac{de(t)}{dt}]$$

(1)

e(t) is the error signal, u(t) is the controller output, K_c is the controller gain, τ_i and τ_d are integral gain and derivative gain. Proportional term speeds up the response as the closed loop time constant decreases with the proportional term but does not change the order of the system as the output is just proportional to the input. The proportional term minimizes but does not eliminate the offset .Integral term eliminates the offset as it increases the type and order of the system by one. This term also increases the system response speed but at the cost of sustained oscillations. Derivative term primarily reduces the oscillatory response of the system. It neither changes the type and order of the system nor affects the offset. Determining optimum value of Proportional constants k_p, τ_i, τ_d is termed as tuning. Any change in these parameters cause changes in the type, order and response of the system. Thus they play a vital role in obtaining a

good controller performance characteristics. There have been a various types of tuning techniques applied for PID controller. One of the oldest is that Zeigler Nichols technique. These techniques may be of Optimization technique or classical technique. Classical techniques make certain assumptions about the plant and the desired output and try to obtain analytically, or graphically some feature of the process that is then used to decide the controller settings. These techniques are computationally very fast and simple to implement, and are good as a first iteration. But due to the assumptions made, the controller settings usually do not cope up with non linear behavior of the process and are unable to give desired response at all operating points which then requires further fine tuning. One of the most successful and oldest classical techniques is Zeigler Nichols method. It was put forward by John Ziegler and Nathaniel Nichols in 1942 and is still a simple, fairly effective PID tuning method. He proposed two methods, one is open loop step response method and the second is closed loop frequency response method. The Ziegler and Nichols first PID tuning method is the techniques made based on certain controller assumptions. Hence, there is always a requirement of further tuning; because the controller settings derived are rather aggressive and thus result in excessive overshoot and oscillatory response. Also the controller parameters are rather difficult to estimate in noisy environment. The second method is based on knowledge of the response to specific frequencies. The idea is that the controller settings can be based on the most critical frequency points for stability. This method is based on experimentally determining the point of marginal stability. This frequency can be found by increasing the proportional gain of the controller, until the process becomes marginally stable. These two parameters define one point in the Nyquist plot. The gain is called ultimate gain K_u and the time period T_p . As the process exhibits non linear behavior at various operating points, this paper aims at fine tuning of the controller settings can be done by computational techniques such as genetic algorithm. This paper is organized as follows. The section 2 describes about literature review of Genetic Algorithm for PID tuning. Section 3 explains about the mathematical modeling of the non-linear spherical tank process. Section 4 describes the Experimental set up and its real time implementation of conventional PID controller and GA tuned PID controller. Section 5 describes the Results obtained for servo operation at various operating points of the tank for both ZN PID controller and GA tuned PID controllers. Finally the conclusion is given in section 6.

II. GENETIC ALGORITHM.

Genetic algorithm (GA) is a search algorithm that explores the search space in a manner analogous to evolution in nature *Salami.M and Cain.G(1995)*. It uses probabilistic rules to search for and change the potential solutions in the search space, using a cost function to analyze the fitness of solutions. GA requires the solution

to be represented in a way that is analogous to genes so that the processes that bring about a change in the genes can be used. Usually this is done by representing the solutions in a binary format.

GA is very popular in PID tuning and has gained wide applications in control systems *Kumar.S.M.G, Jain.R and Anantharaman.N.(2008)*. *Sadasivarao.M.Vand Chidambaram,(2006)* uses GA for improving performance of a PID controller used in bioreactor and compared the performance with Ziegler Nichols, Skogestad modification *Skogestad.S.(2003)* found that GA outperformed both in terms of overshoot, disturbance rejection, gain margin and phase margin. GA has been used in position and speed control of a DC motor *NeenuThomas P. Poongodi(2009)*. *SharifianM.B.B.Rahnavard.RandDelavari.H(2012)*. GA has been used for PID of reverse osmosis *Jin-Sung Kim, Jin-Hwan Kim, Ji-Mo Park, Sung-Man Park, Won-YongChoe and Hoon Heo,(2008)* and cascade control systems tuning in *Sadasivarao.M.V and Chidambaram,(2006)*. Lot of work has been done in using GA along with other computational techniques. In *Kim et al.* uses bacteria forage along with GA for PID controller tuning of AVR systems. GA was used with Neural Networks *Dolezel, PetrMares,(2009)* and with fuzzy logic for developing self tuning methods.

III. MATHEMATICAL MODELLING

A spherical tank system, shown in figure 1 is essentially a system with non linear dynamics. The spherical tank system has a maximum height of 0.5meter and the maximum radius of 0.5 meter. The level of the tank at any instant is measured by the combination of orifice and Differential pressure transmitter whose output is (4 - 20)mA. This output is compared with the desired set point value of level which will be configured as (4 - 20)mA. The error signal is amplified based on the controller specification. The controller output is used to vary the inflow rate $q_1(t)$ of the spherical tank so as to maintain the set point at desired level of the tank. An Electro pneumatic converter is used to convert the controller output of (4 -20)mA in to a pneumatic signal of (3-15) psi so that the final control element will be able to throttle the inflow rate.

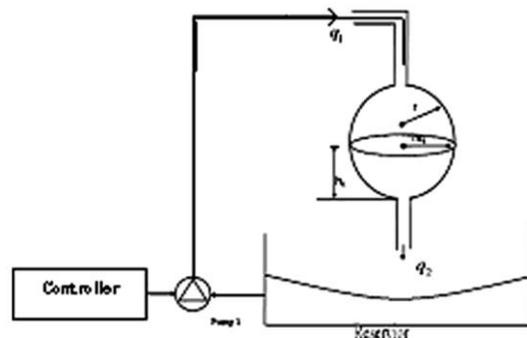


Figure 1. Schematic diagram of Spherical Tank process

let, $q_1(t)$ - inlet flow rate to the tank in m^3/sec
 $q_2(t)$ - outlet flow rate of the tank in m^3/sec
 H - Height of the spherical tank in meter.
 R - Radius of tank in meter (0.5 meter).
 x_0 - Thickness of pipe in meter(0.04 meter).

Using law of conservation of mass the non-linear plant equation is obtained for the spherical tank,

$$q_1(t) - q_2(t) = A(h_1) \frac{dh_1}{dt} \quad (2)$$

Where, $A = \pi r_{surface}^2$

Radius on the surface of the fluid varies according to the level (height) of fluid in the tank. Let this radius be known as $r_{surface}$.

$$r_{surface} = \sqrt{2rh_1 - h_1^2}, A = \pi(2rh_s - h_s^2) \quad (3)$$

And

$$q_2(t) = a\sqrt{2g(h - x_0)}, \text{ where } a = \pi(x_0/2)^2 \quad (4)$$

Substituting (3) and (4) in equation (2) and linearizing the non linearity in spherical tank gives rise to a transfer function of

$$Q_1(s) - \frac{a\sqrt{2g}H(s)}{2\sqrt{h_s - x_0}} = \pi(2rh_s - h_s^2)SH(s) \quad (5)$$

Rearranging,

$$\frac{H(s)}{Q(s)} = \frac{1}{\pi(2rh_s - h_s^2)S + \frac{a\sqrt{2g}}{2\sqrt{h_s - x_0}}} \quad (6)$$

Applying the steady state condition values, the linearized plant transfer function is given by,

$$\frac{Y(s)}{U(s)} = \frac{0.59}{S + 0.004} \quad (7)$$

IV. EXPERIMENTAL SET UP OF SINGLE SPHERICAL TANK PROCESS



Fig. 2. Experimental set up for single spherical tank system.

The experimental set up of the single spherical tank system is shown in figure 2. The spherical tank is made up of SS316 material which has high corrosion resistance property and has a maximum height and radius of 0.5 meter. Water from the reservoir tank of size 1250mm x 450mm x 450mm is pumped through a Kirloskar make 0.5 HP pump having a discharge of 1500 litres per hour that flows through a Teleline make rotameter having a range (40 - 440)LPH to the spherical tank. The level of the tank at any instant is measured by the Rose mount Differential pressure transmitter having a measurement range of (0-400)mm of water column corresponds to the output range of (4 -20)mA. This output is compared with the desired set value of level which will be scaled in the control law as (4 -20)mA. The error signal is also in the range of (4-20)mA which is then amplified based on the controller specifications. This output is used to vary the inflow rate $q_1(t)$ of the spherical tank with the use of an ABB make Electro pneumatic converter which converts the output of (4 -20)mA in to a pneumatic signal of (3-15) psi so that the Equal percentage control valve will be able to throttle the inflow rate. The controller parameters are determined for both ZN tuned PID Controller as well as GA tuned PID controllers. The values of k_p , k_i , k_d for ZN tuned PID are found to be 0.33, 0.036, 0.7623 respectively. An USB 6009 NI Data acquisition card is use to communicate the data from the transmitters to the PID controller block of LabVIEW program both for ZN and GA tuned control algorithm to perform its operation for a given step change in inflow rate q_i , and the corresponding steady state response is obtained as follows.

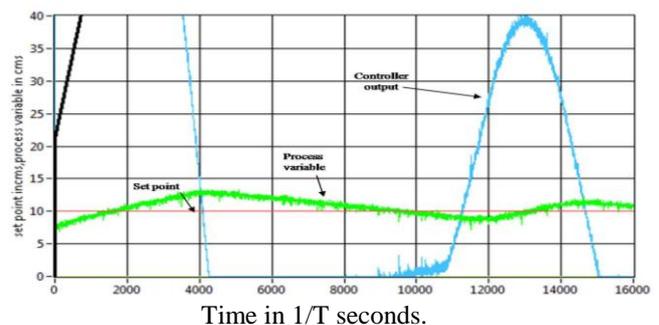


Fig. 3. Response of ZN tuned PID controller for a set point of 10cms of water column.

It is evident from the response that the ZN tuned PID controller output could track the set point at an operating point of 10cms of water column with a settling time of 13.15seconds and with minimal overshoots where the sampling rate T is 32samples per second.

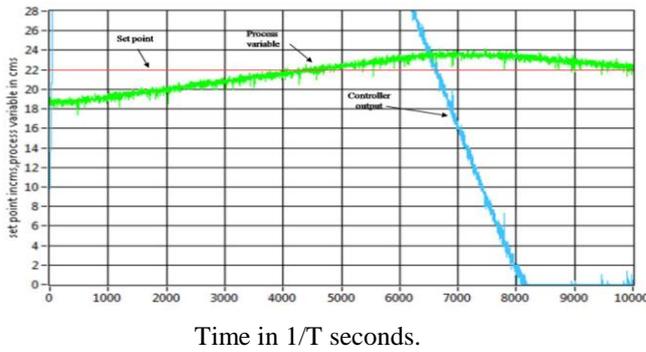


Fig. 4. Response of ZN tuned PID controller for a set point of 22cms of water column.

It is evident from the response that the ZN tuned PID controller output could track the set point at a different operating point of 22cms of water column with a settling time of 8.22seconds and with minimal overshoots where the sampling rate T is 32samples per second.

A. GA based PID controller

Genetic algorithms (GA) are an evolutionary optimization approach, which are an alternative to traditional optimization methods. GA is one of the most appropriate methods for complex non-linear models where location of the global optimum is a difficult task. GA follows the concept of solution evolution by stochastically developing generations of solution populations using a given fitness. Genetic algorithms are a probabilistic search approach, which are founded on the ideas of evolutionary processes. The GA procedure is based on the Darwinian principle of survival of the fittest. An initial population is created containing a predefined number of individuals, each represented by a genetic string. Each individual has an associated fitness measure. The concept that the fittest best individuals in a population will produce a fitter offspring is then implemented in order to reproduce the next population. Selected individuals are chosen for reproduction at each generation, with an appropriate mutation factor to randomly modify the genes of an individual, in order to develop the new population. The result is another set of individuals based on the original subjects leading to subsequent populations with better fitness and those with lower fitness will naturally get discarded from the population. (Goldberg 1989; Lewin 1994, 1996). For most applications of genetic algorithms to optimization problems, the real coding technique is used to represent a solution to a given problem. In real coding implementation, each chromosome is encoded as a vector of real numbers, of the same lengths as the solution vector. According to control objectives, three parameters K_p , K_i and K_d of a PID controller are required to be designed in this research. For a given problem with three decision variables, this paper adopts a real-valued vector $[x_1, x_2, x_3]$ as a chromosome to represent a solution to the problem.

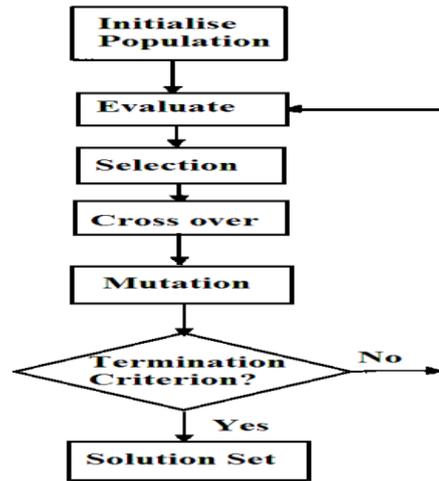


Fig. 5. General Flow chart of Genetic Algorithm

B. Tuning of GA-Based PID Controller

Genetic Algorithm can naturally be applied to the optimal-tuning of PID controllers as a mathematical means for optimization. The role of the PID controller in a system is to drive the output response to track the set point within minimum settling time. Obviously, the parameter settings of the PID controller should be fine tuned so as to meet the requirements. Optimization of PID controllers firstly needs design the optimization goal, and then encode the parameters to be searched. Genetic operator is running until the stop condition is satisfied. The decoded values of the last chromosome are the optimized PID controller parameters.

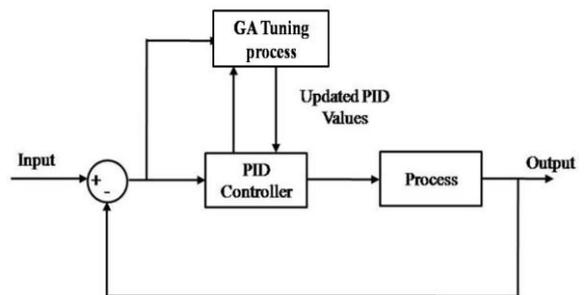


Fig. 6. Schematic diagram of GA based PID tuning a process

Initially a chromosome is randomly generated. The chromosomes are candidate solutions to the problem. The fitness values of all chromosomes are evaluated by calculating the objective function (ISE) in decoded form. Hence, based on the fitness of each individual, a group of the best chromosomes is selected through the selection process. The Genetic operators, crossover and mutation, are applied to this surviving population in order to improve the next generation solution. The process

continues until the population converges to the global maximum or another stopping criterion is reached. The GA optimization tool in matlab is used to fine tune the PID parameters so as to obtain the desired performance characteristics. The following figure 7 shows the Optimization wizard for GA tuned PID controller. The fitness function syntax is developed as a function and saved with a file name Sphh. Then the other parameters such as lower bounds, upper bounds, number of variables, Initial population, Initial range, number of iteration, Mutation factor, Cross over factor and selection function are given to the wizard. On running the program, it determines an optimal set of tuned parameters for PID controller as $k_p=6.997, \tau_i=6.144\text{sec}$ and $\tau_d=1.998\text{sec}$.

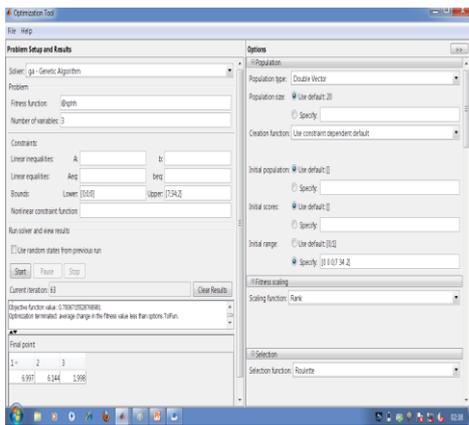


Fig. 7. Optimization wizard for GA tuned PID controller

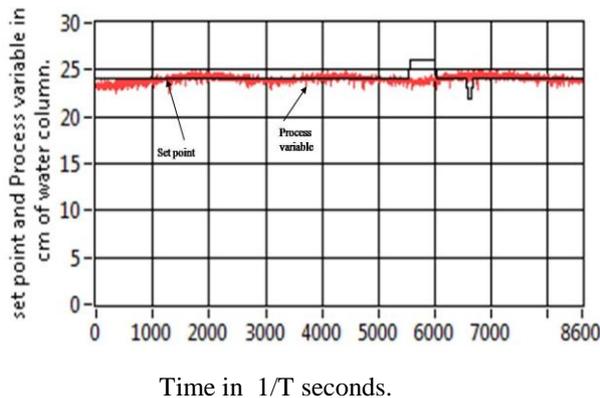


Fig. 8. Response of GA tuned PID controller for a set point of 24cms of water column.

It is evident from the response that the GA tuned PID controller output could track the set point at a different operating point of 24cms of water column with a settling time of 7.13seconds and with smooth response and no overshoots where the sampling rate T is 32samples per second. A small disturbance is being provided between the time instances 5000,6000,and 7000 so as to ensure robustness, the controller ensures disturbance rejection and it keep tracks the set point value as desired.

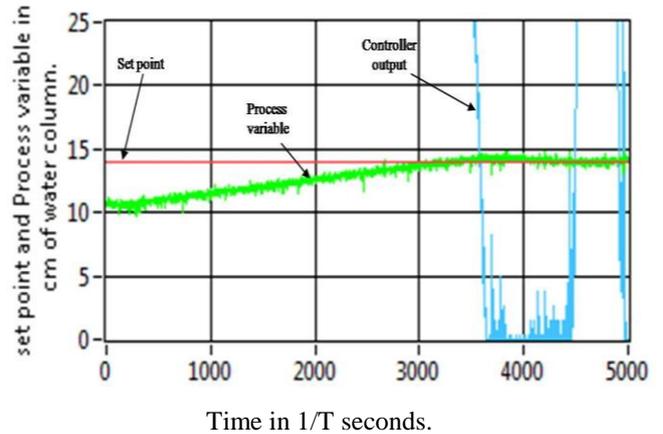


Fig. 9. Response of GA tuned PID controller for a set point of 14cms of water column.

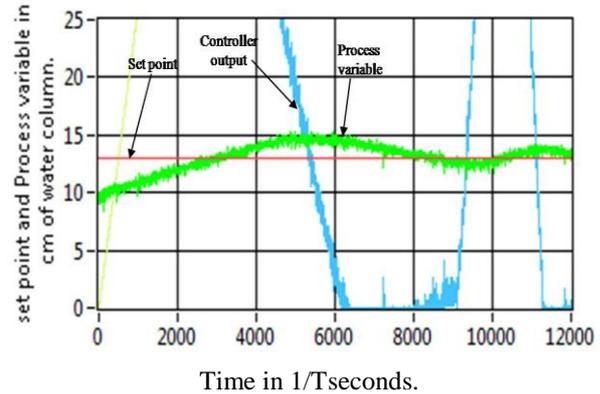


Fig. 10. Response of GA tuned PID controller for a set point of 13cms of water column.

It is evident from the response that the GA tuned PID controller output could track the set point at a different operating point of 14cms of water column with a settling time of 4.53seconds and with smooth response and no overshoots where the sampling rate T is 32samples per second.

V. RESULTS AND DISCUSSION

An unit step response of ZN tuned PID controller and GA tuned PID controller is obtained for servo operations and their performance characteristics are compared in terms of time domain specifications such as rise time ,peak time, peak over shoot, steady state value etc., and performance indices such as ISE and IAE. Table 1 and table 2 show characteristics of time domain specification and performance indices such as ISE and IAE of ZN tuned PID controller against GA tuned PID Controller.

Table1

Type of contr	Set point in cms	Settling time in seconds	Max Peak over shoot %	Peak time in seconds	Steady State Value.
ZN PID	10	14.1	20.9	3.96	10.99
	22	44.56	9.702	40.95	21.98
GA PID	14	4.53	5.8824	0.44	13.945
	24	7.13	4.1096	0.75	23.953

Table2

Type of controller	Set point in cms	Integral Square Error	Integral Absolute Error
ZN PID	10	19605	2801.7
	22	12539	7090.7
GA PID	14	37359	3869
	24	19992	8953

VI. CONCLUSION

GAPID controller can cope up with tank non-linear characteristics at various operating points such as 14, 24centimeters of water column in the spherical tank. Conventional controller based on Ziegler Nichols tuning response is outperformed by GAPID controller with less overshoot and lesser settling time, peak time etc.,. GA tuned PID controller is the basic evolutionary computational method which provides a better satisfactory results as tabulated. The author limited his work with GA based tuning alone, further the controller can be tuned by other soft computing techniques and implemented in real time so as to compare their performances. GAPID controller can also be applied for other non linear processes such as Continuous stirred tank reactor, Yeast fermentation process, Bio reactor etc to obtain better controller performance characteristics.

REFERENCES

[1] Astrom.K.J and Hagglund.T,(1995).”PID controllers, Theory, design and tuning” 2nd edition, *Instrument Society of America*, 1995.

[2] Astrom.K.J and Hagglund.T,(1991).Industrial Adaptive Controllers Based on Frequency Response Techniques, *Automatica.*, 27(4) 599-609.

[3] AnnaJoseph,J.SamsonIsaac(2013).Real time Implementation of Model Reference Adaptive Controller for a conical Tank.,*International Journal on theoretical and applied research in Mechanical Engineering*,2(1).

[4] Abdel Badie Sharkawy,(2006) Genetic fuzzy self-tuning PID controllers for Antilock Braking Systems, *Alexandria Engineering Journal*, vol. 45(6) .657-673.

[5] Dolezel, PetrMares,(2009)Self tuning PID Control using Genetic Algorithm and Artificial Neural Networks,” *ASR Instruments and Control*, pp. 33- 39, 2009.

[6] Dong Hwa Kim, Jae Hoon Cho.(2006)A Biologically Inspired Intelligent PID Controller Tuning for AVR Systems.*International Journal of Control, Automation, and Systems.* 4(5) 624-636.

[7] Jin-Sung Kim, Jin-Hwan Kim, Ji-Mo Park, Sung-Man Park, Won-YongChoe and Hoon Heo,(2008)Auto Tuning PID Controller based on Improved Genetic Algorithm for Reverse Osmosis Plant, *International Journal of Computer Systems Science and Engineering.*, 3(4),232 – 237.

[8] Kumar.S.M.G. Jain.R and Anantharaman.N.(2008) Genetic Algorithm Based PID Controller Tuning for a Model Bioreactor. *Indian Chemical Engineering Journal.* 50,(3). 214-226.

[9] NeenuThomas P. Poongodi(2009) Position Control of DC Motor Using Genetic Algorithm Based PID Controller, *Proceedings of the World Congress on Engineering, London,U.K.*,vol. 2., 1618-1622.

[10] Sadasivarao.M.V and Chidambaram,(2006)PID Controller tuning of cascade control systems using genetic algorithm, *Journal of Indian Instrumentation Science.* vol. 86., 343–354.

[11] Salami.M and Cain.G(1995) An Adaptive PID Controller Based on Genetic Algorithm Processor. *IEEE Genetic Algorithms in Engineering Systems, Innovations and Applications Conference.* 12-14.

[12] SharifianM.B.B.Rahnavard.RandDelavari.H(2012) Velocity Control of DC Motor Based Intelligent methods, *Journal of Control Engineering and Technology*,2 (4). 168-176.

[13] Skogestad.S.(2003) Simple Analytic Rules for Model Reduction and PID Controller tuning. *Journal of Process Control*,(13). 291-309.

[14] PradeepKannan.D, Sathiyamoorthy,(2012) Design and Modelling of State Feedback with Integral Controller for a Non-Linear spherical tank Process., *International Journal of Emerging Technology and Advanced Engineering*, 2(11),.668-672.

[15] Ziegler.J.G and Nichols..N.B,(1942).Optimum Settings for Automatic Controller. *Transaction of ASME.* 64. 759-768.

BIOGRAPHIES



D.Pradeep kannan received his Bachelors Degree in Instrumentation and Control Engineering from Madurai Kamaraj University,India. in 1999and Master degree in Industrial Engineering in 2001 from Madurai kamaraj University..Currently he is an Associate professor in the department of Electronics and Instrumentation Engineering in K.L.N. College of Engineering, Madurai, India. He is pursuing his Research program at Anna University Chennai India.He has published about 4 papers in reputed Journals andConferences. His research interests includes Process control,Fraction order PID controllers,Tuning of controllers for nonlinear processes using soft computing techniques etc. He is a life member of ISTE and ISOI societal bodies.His mail id is pradip_eie@yahoo.co.in.



Dr.S.Sathiyamoorthy, Principal of J.J. College of Engineering and Technology has sixteen years of experience in teaching, research and industry. He has completed B.E. Degree in Electrical and Electronics Engineering, Regional Engineering College, Tiruchirapalli in 1995, and M.E. degree in Control and

Instrumentation at Guindy Engineering College, Anna University, Chennai in 2002. He has received his Doctorate from National Institute of Technology, Tiruchirapalli in 2008. He has attended many National and International conferences and workshops. He has published five papers in leading international journals. He has given numerous expert lectures in various forums and Colleges in area of Neural Networks and Fuzzy logic control. His area of specialization are Process Control and Industry Automation, Multiphase flow identification using Electrical Capacitance Tomography.